

# Progress in Aerodynamic Shape Optimization

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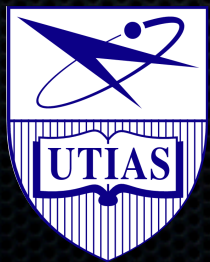
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# OUTLINE

- ▶ Turbulent flow solver
  - Summation-by-parts/simultaneous approximation terms
  - parallel Newton-Krylov-Schur algorithm
- ▶ Integrated geometry parameterization and mesh movement
- ▶ Adjoint-based gradient computation
- ▶ Turbulent flow solver
- ▶ Global optimization algorithms

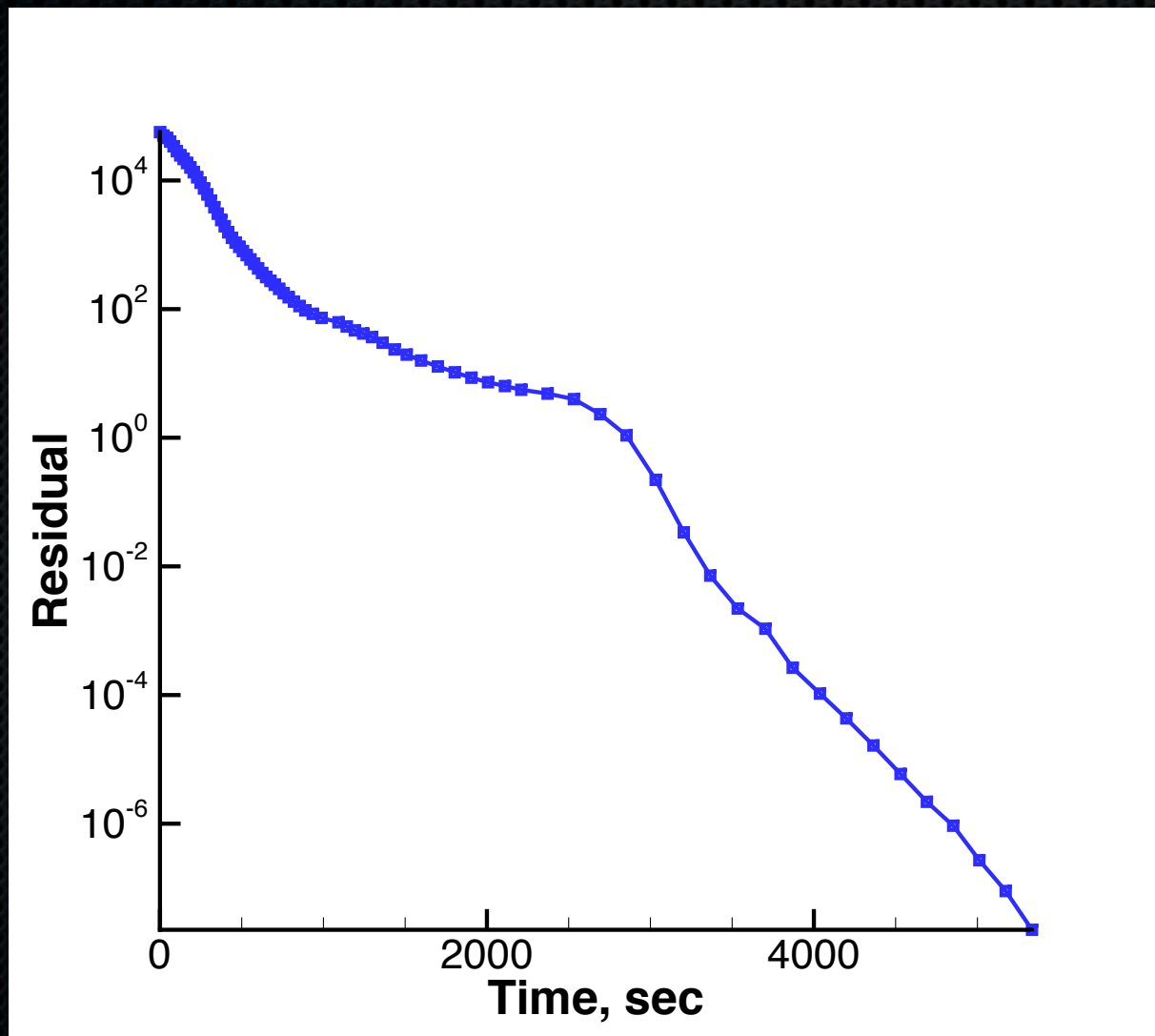
# FLOW SOLVER

- Structured multi-block grids
  - High-order finite-difference method with summation-by-parts operators and simultaneous approximation terms
  - Parallel Newton-Krylov-Schur solver
  - Jacobian-free Newton-Krylov algorithm with approximate Schur parallel preconditioning
  - Promising dissipation-based continuation method for globalization
- ➔ Hicken, J.E., and Zingg, D.W., A parallel Newton-Krylov solver for the Euler equations discretized using simultaneous approximation terms, AIAA Journal, Vol. 46, No. 11, 2008
- ➔ Osusky, M., and Zingg, D.W., A parallel Newton-Krylov flow solver for the Reynolds-Averaged Navier-Stokes equations, AIAA ASM, Jan. 2012

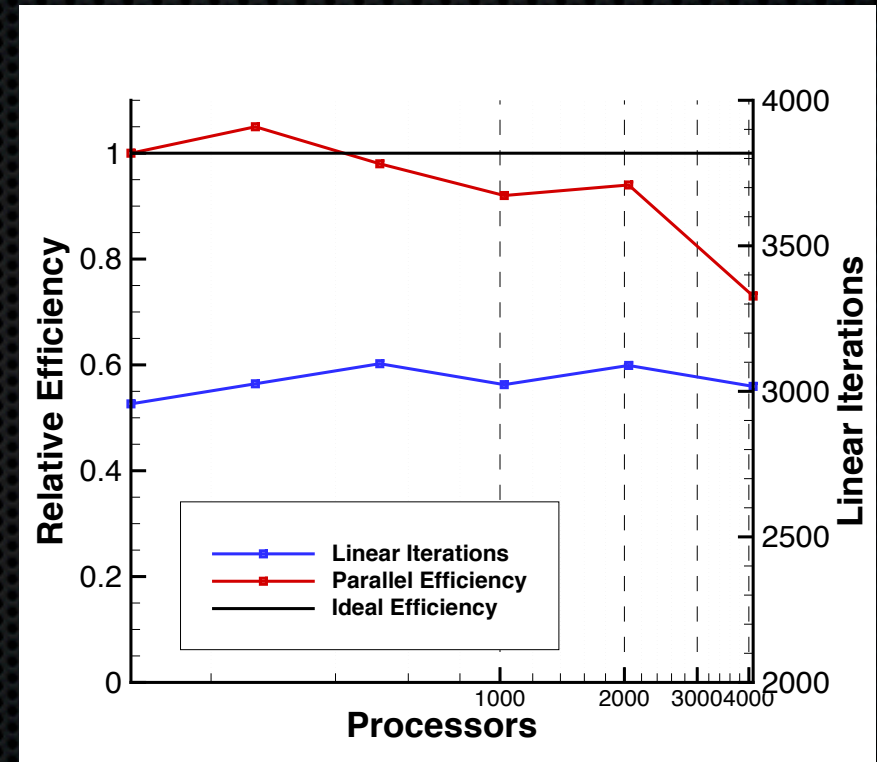
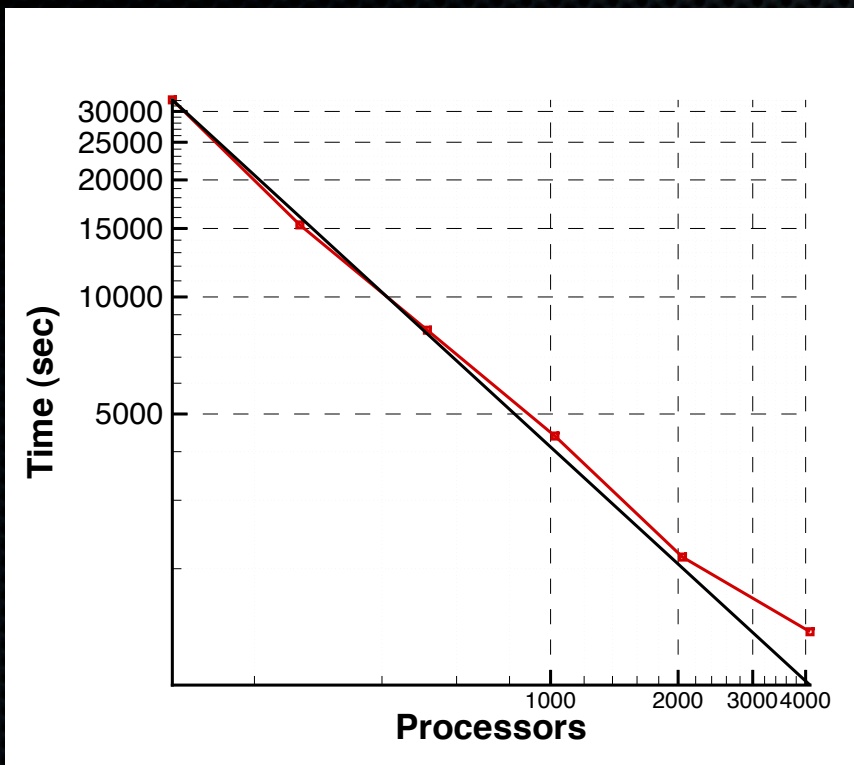
# Turbulent Flow Solver

ONERA M6 wing:  $M=0.8395$ ,  $\alpha=3.06$  degrees

$Re=11.72$  million, 15.1 million mesh nodes, 128 processors



# Parallel Scalability (RANS)



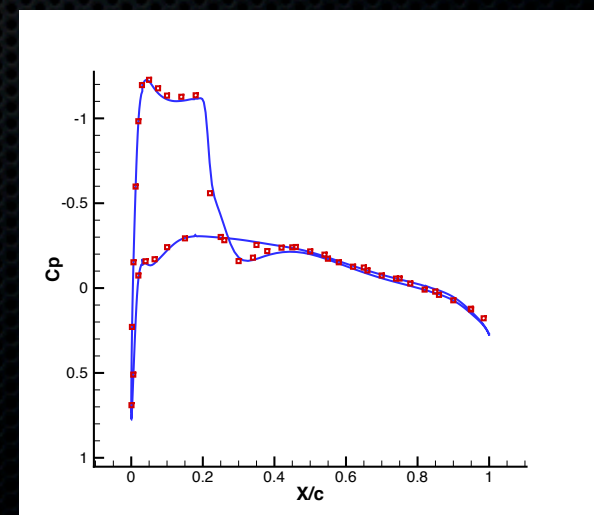
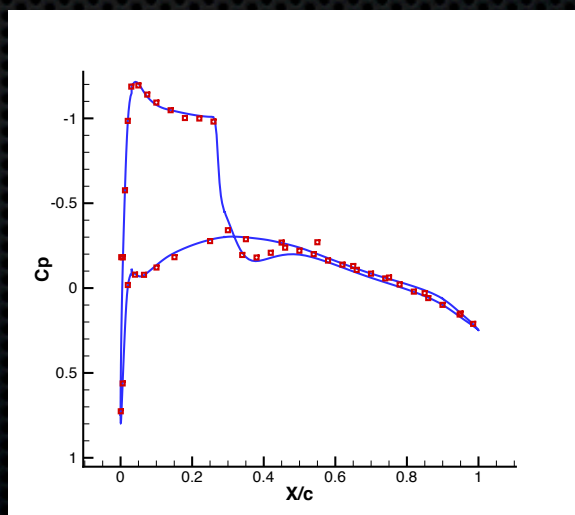
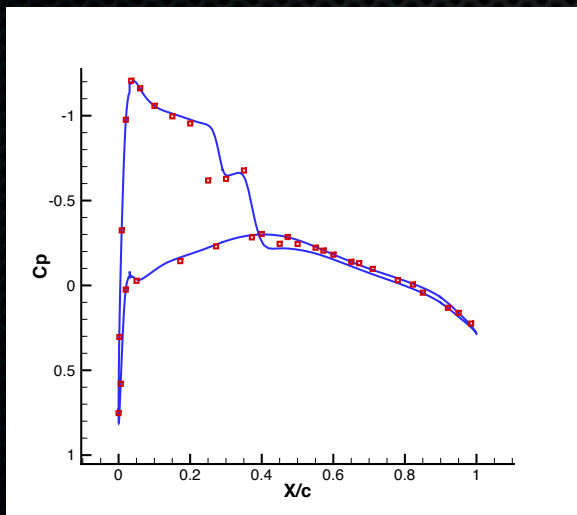
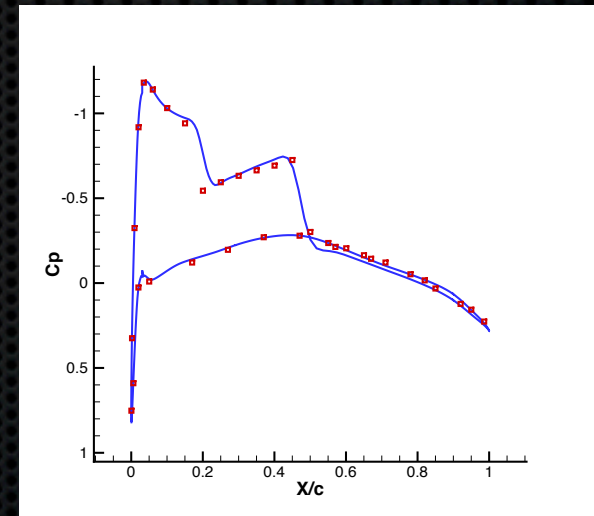
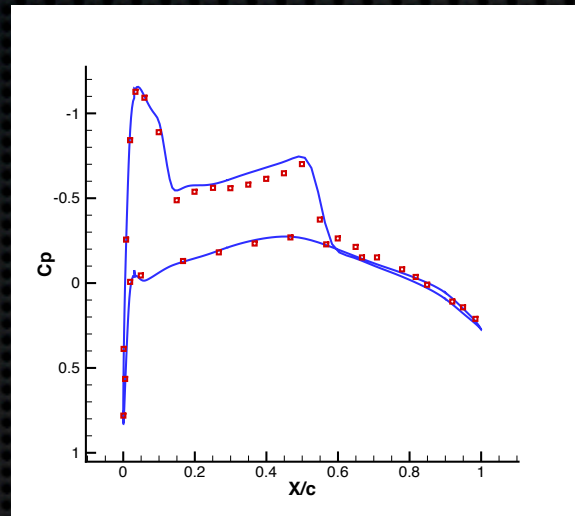
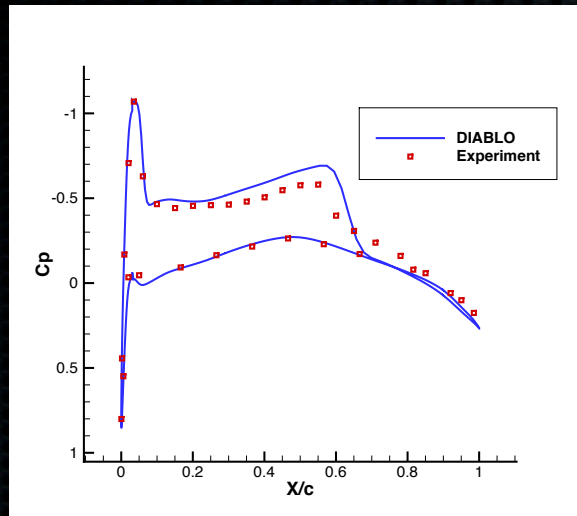
- 12 order residual reduction in 23 mins on 4096 processors (40 million mesh nodes)

# Turbulent Flow Solver

ONERA M6 wing:  $M=0.8395$ ,  $\alpha=3.06$  degrees

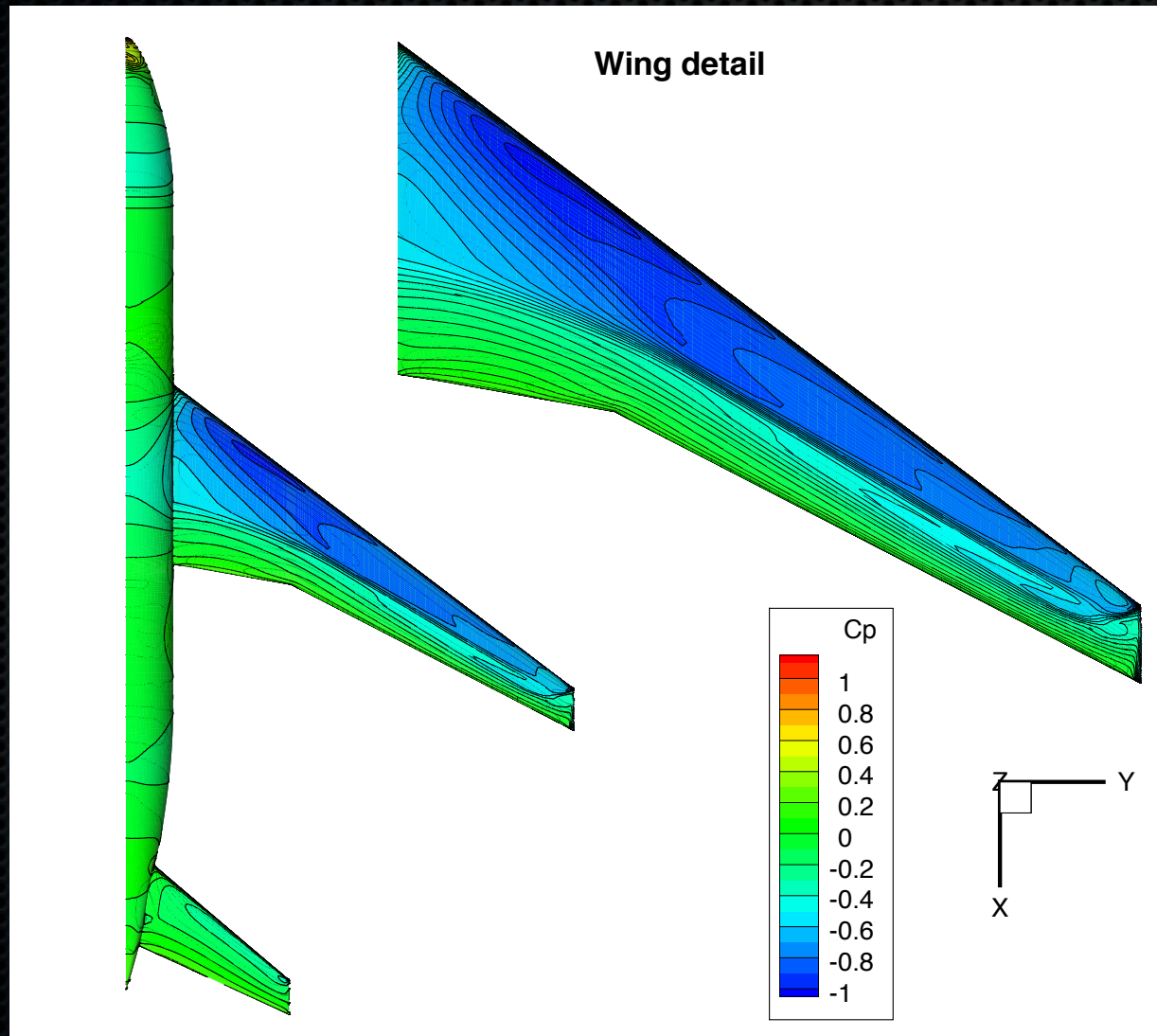
$Re=11.72$  million, 15.1 million mesh nodes

20, 44, 65, 80, 90, 95 percent span



# Turbulent Flow Solver

Common Research Model:  $M=0.85$ ,  $C_L=0.5$   
 $Re=5$  million, 10.1 million mesh nodes

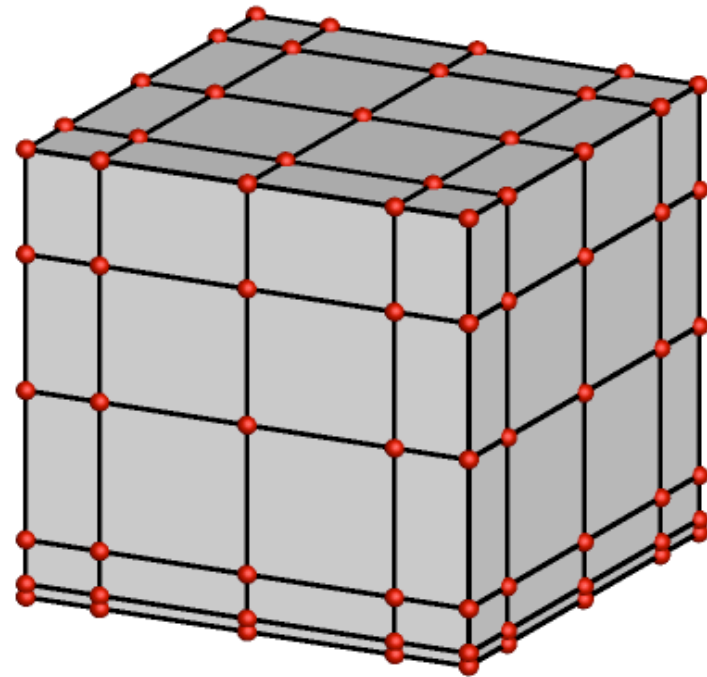
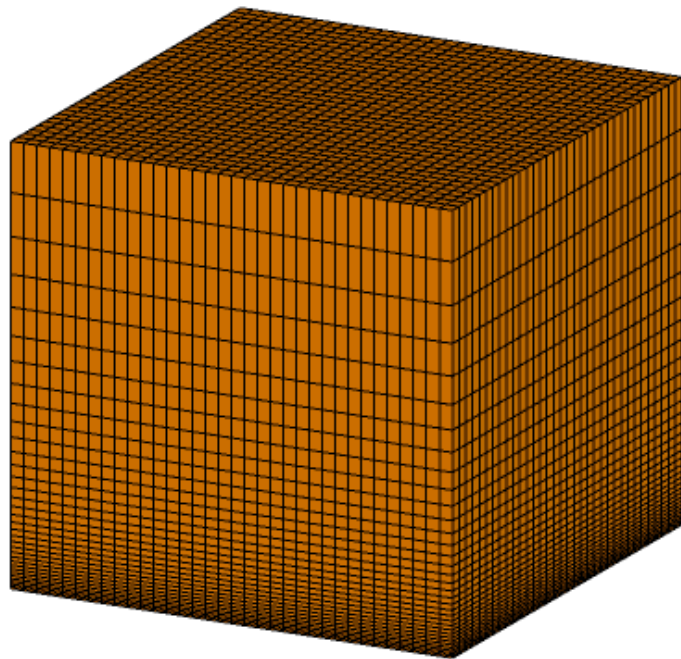


# INTEGRATED GEOMETRY PARAMETERIZATION AND MESH MOVEMENT

- Must provide flexibility for large shape changes with a modest number of design variables
    - ▶ B-spline patches represent surfaces
    - ▶ B-spline control points are design variables
  - Mesh movement must maintain quality through large shape changes
    - ▶ through tensor products, B-spline volumes map a cube to an arbitrary volume with the appropriate topology
    - ▶ can be arbitrarily discretized in the cube domain to create a mesh
    - ▶ B-spline volume control points can be manipulated to move the mesh in response to changes in the surface control points
    - ▶ efficiently generates a high quality mesh
- ➔ Hicken, J.E., and Zingg, D.W., Aerodynamic Optimization Algorithm with Integrated Geometry Parameterization and Mesh Movement, AIAA Journal, Vol. 48, No. 2, 2010

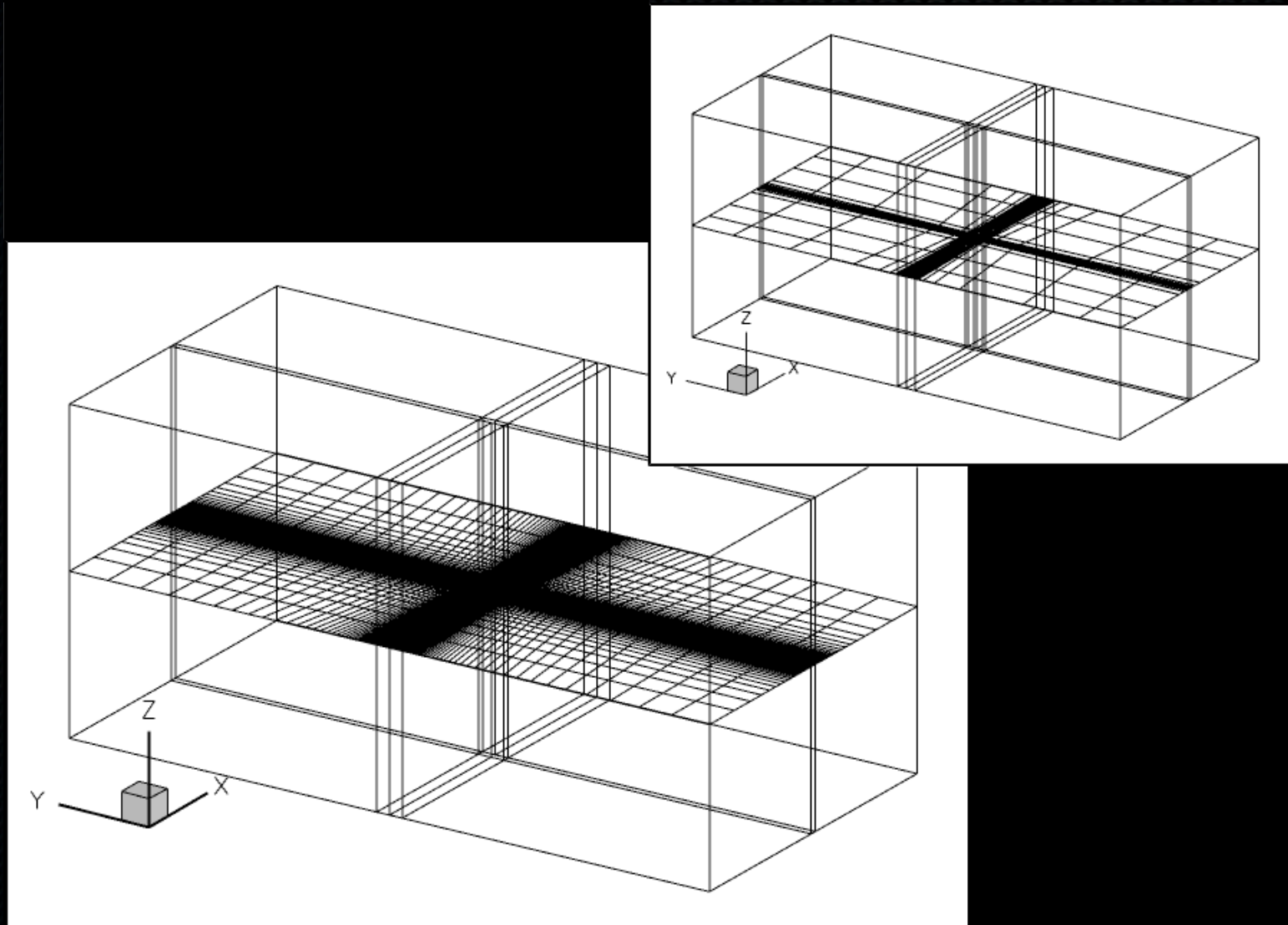


# B-spline Volumes



# Mesh Movement Example

flat plate to blended-wing body:  $\approx 1$  million nodes



# DISCRETE-ADJOINT GRADIENT COMPUTATION

- Cost independent of the number of design variables
  - Efficient if the number of design variables exceeds the number of constraints
  - Hand linearization complemented by judicious use of the complex step method for difficult terms
  - Adjoint equation solved by parallel Schur-preconditioned modified Krylov method GCROT(m,k)
- ➔ Hicken, J.E., and Zingg, D.W., A Simplified and Flexible Variant of GCROT for Solving Nonsymmetric Linear Systems, *SIAM Journal on Scientific Computing*, Vol. 32, No. 3, March 2010

# Discrete Adjoint Gradient

Define a Lagrangian function using objective, flow equations, and mesh movement equations

$$\mathcal{L}(\mathbf{v}, \mathbf{q}, \mathbf{b}, \boldsymbol{\psi}, \boldsymbol{\lambda}) = \mathcal{J} + \boldsymbol{\psi}^T \mathcal{R} + \boldsymbol{\lambda}^T \mathcal{M}$$

- $\boldsymbol{\psi}$  and  $\boldsymbol{\lambda}$  are the flow and mesh adjoint variables

At local optima, all derivatives of  $\mathcal{L}$  vanish:

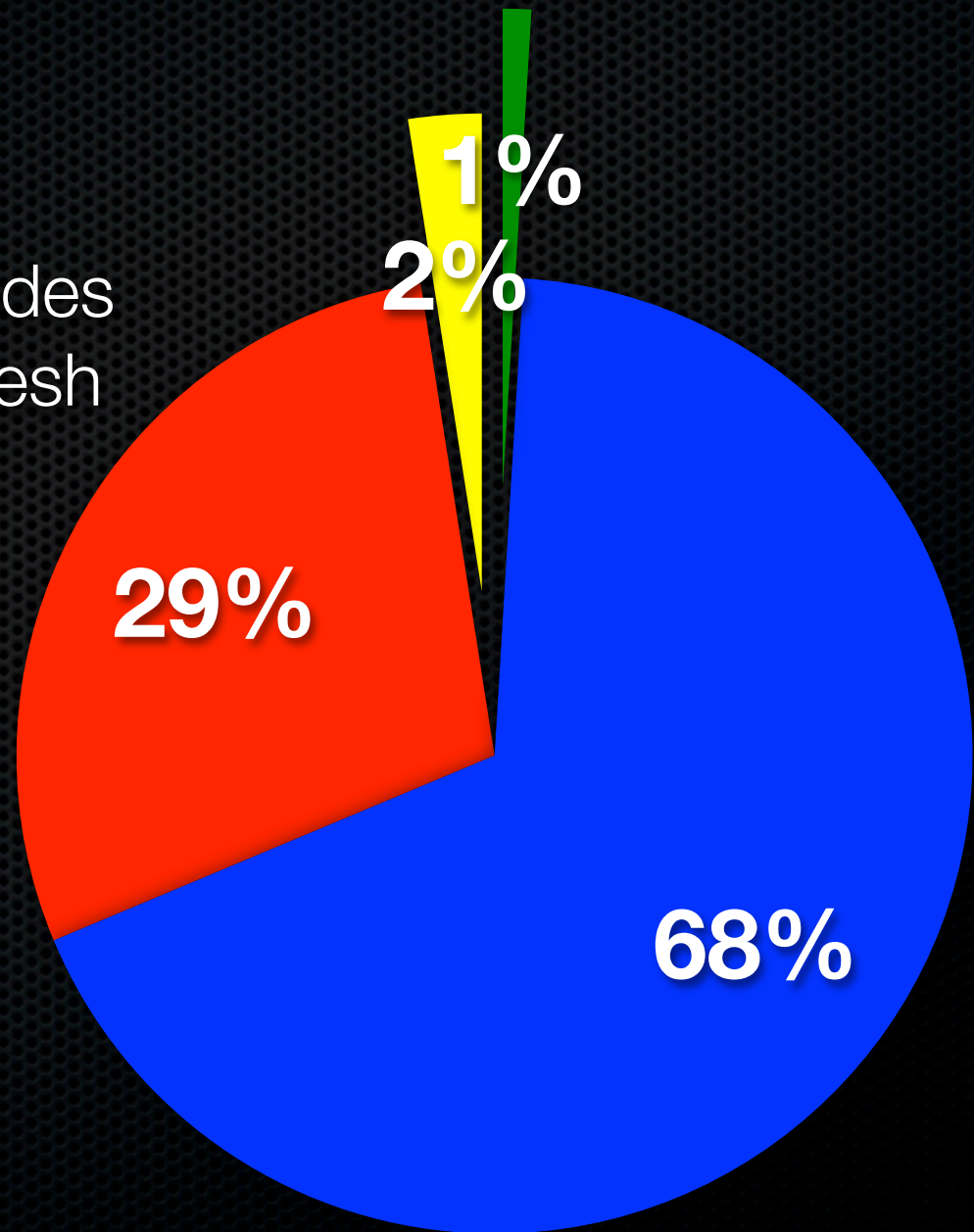
$$\begin{aligned} \frac{\partial \mathcal{L}}{\partial \mathbf{q}} &= \frac{\partial \mathcal{J}}{\partial \mathbf{q}} + \boldsymbol{\psi}^T \left( \frac{\partial \mathcal{R}}{\partial \mathbf{q}} \right) = 0 \\ \frac{\partial \mathcal{L}}{\partial \mathbf{v}} &= \frac{\partial \mathcal{J}}{\partial \mathbf{v}} + \boldsymbol{\psi}^T \left( \frac{\partial \mathcal{R}}{\partial \mathbf{v}} \right) + \boldsymbol{\lambda}^T \left( \frac{\partial \mathcal{M}}{\partial \mathbf{v}} \right) = 0 \\ \frac{\partial \mathcal{L}}{\partial \mathbf{b}} &= \frac{\partial \mathcal{J}}{\partial \mathbf{b}} + \boldsymbol{\psi}^T \left( \frac{\partial \mathcal{R}}{\partial \mathbf{b}} \right) + \boldsymbol{\lambda}^T \left( \frac{\partial \mathcal{M}}{\partial \mathbf{b}} \right) = 0 \end{aligned}$$

# CPU Time Breakdown: one iteration

Example:  $1.16 \times 10^6$  nodes

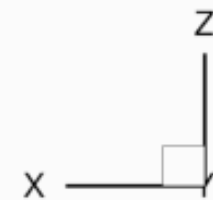
- mesh movement + mesh adjoint: 3%
- gradient: 31%

- mesh move
- flow solve
- flow adjoint
- mesh adjoint



# Application to Wing Design

Lift-constrained induced-drag minimization

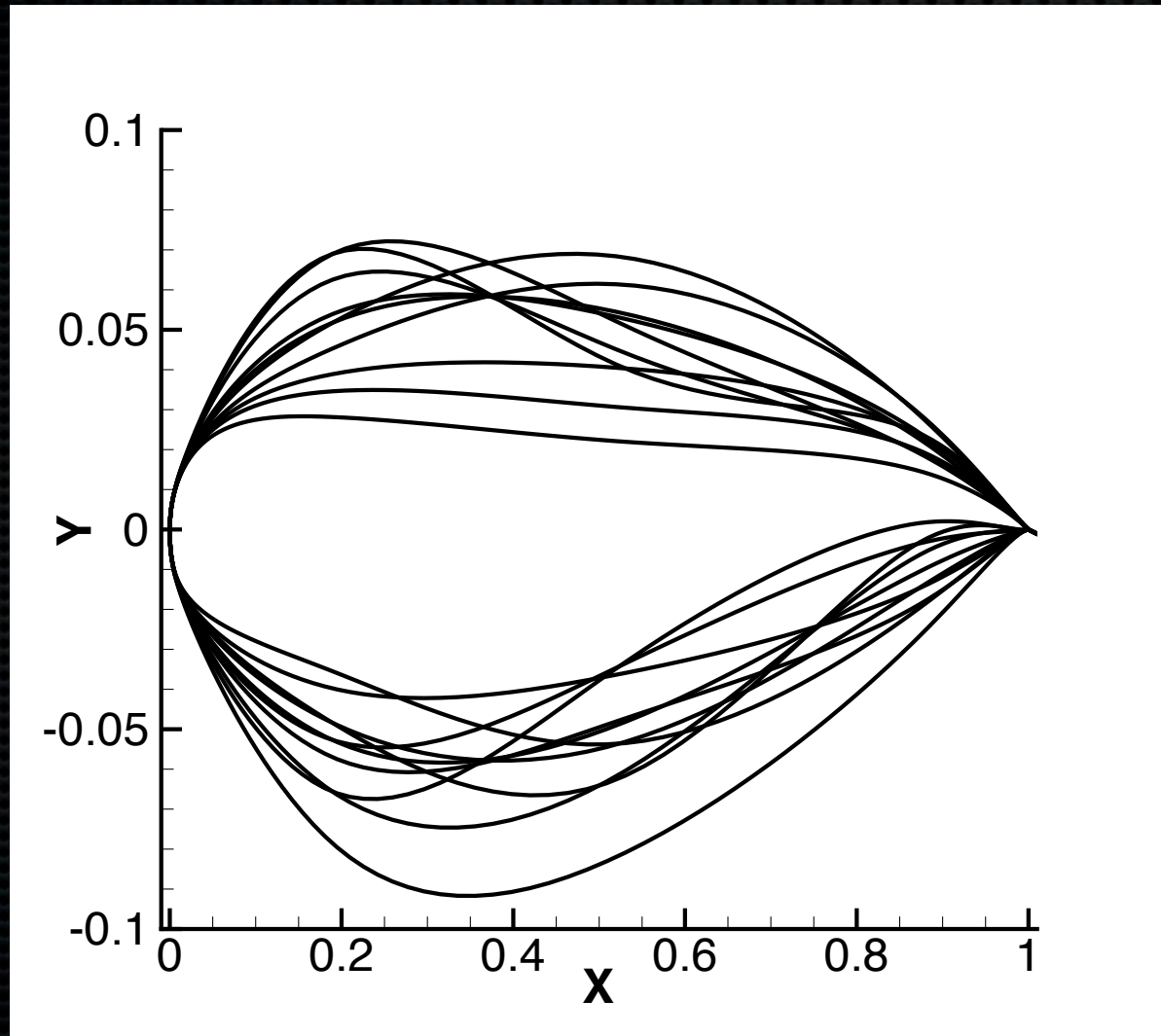


# Global Optimization Algorithms

- Gradient-based algorithm (GB) - converges to a local minimum
- Multi-start Sobol (GB-MS): initial guesses based on Sobol sequences cover the design space in a deterministic manner (sampling in linear feasible region)
- Hybrid method (HM): combination of genetic algorithm, Sobol sampling, and gradient-based algorithm (SNOPT is run on each chromosome)
- Genetic algorithm (GA)

# Multimodality

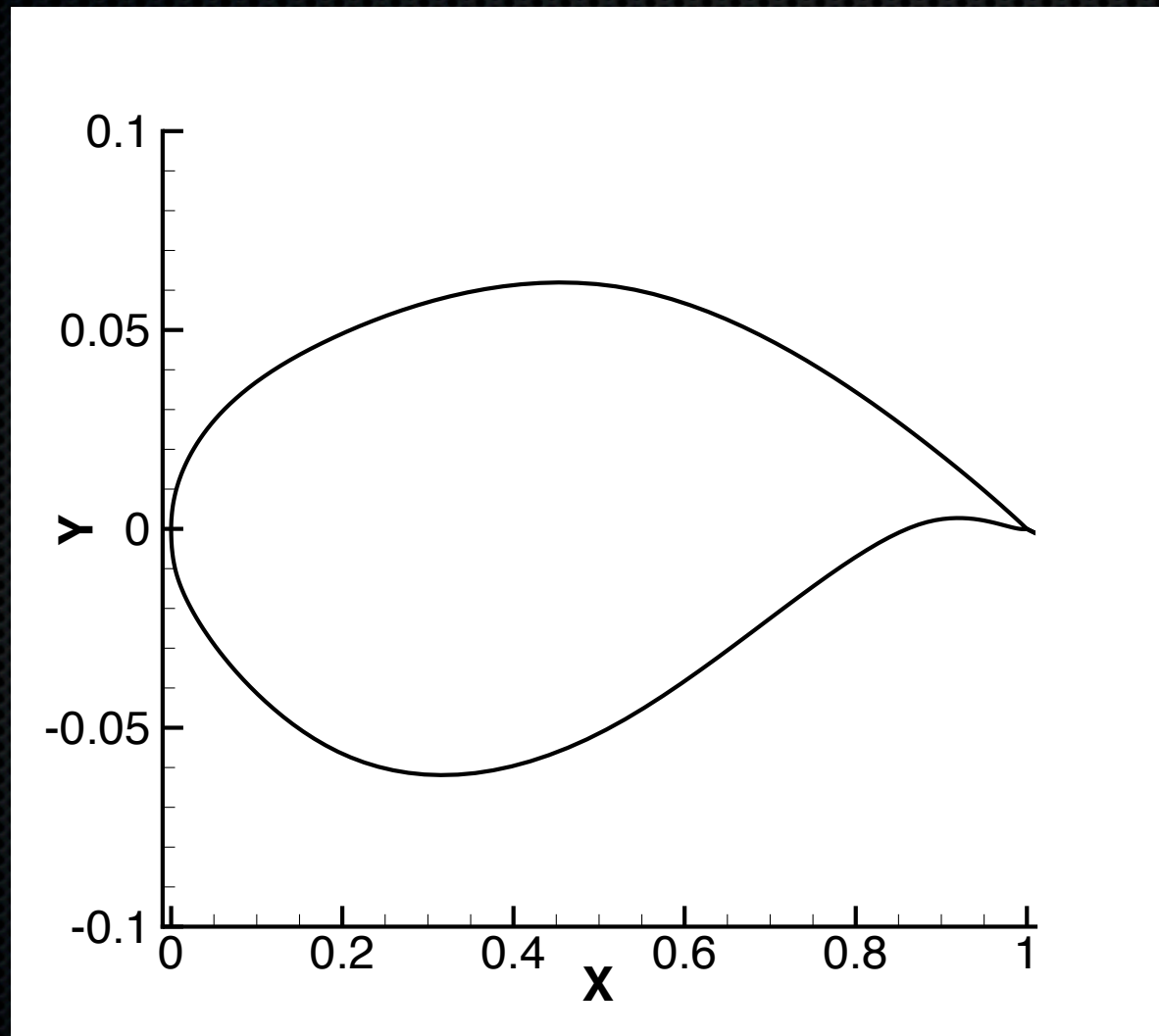
Multistart procedure for 2D airfoil optimization  
(transonic lift-constrained drag minimization, 6 DVs)





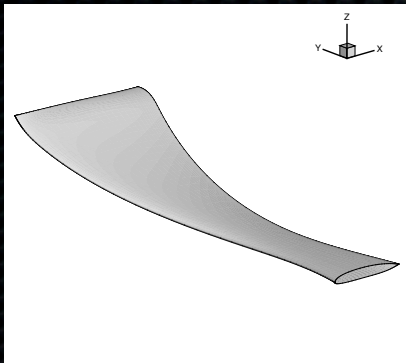
# Multimodality

A unique global optimum in 2D - no local optima!

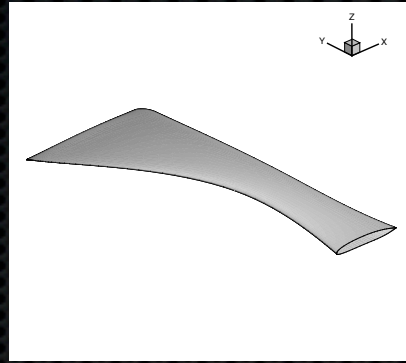


# Multimodality

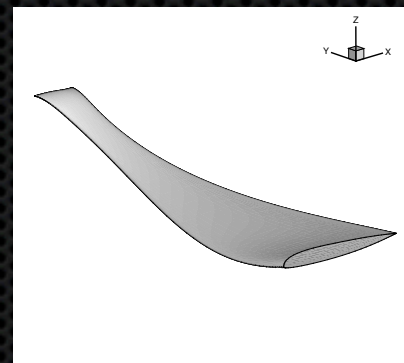
- 3D: subsonic lift-constrained drag minimization, 129 DVs
- 7 local minima found - somewhat multimodal
- GB-MS most efficient



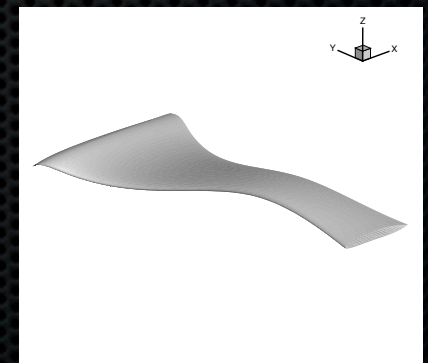
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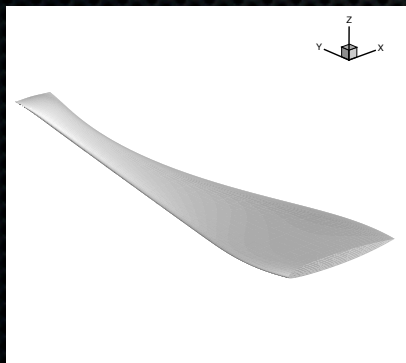
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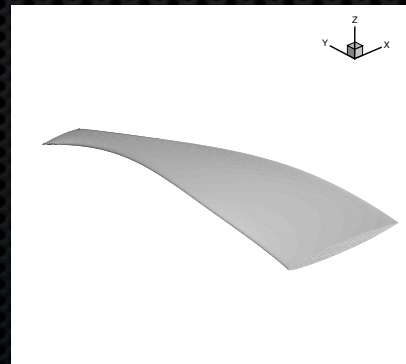
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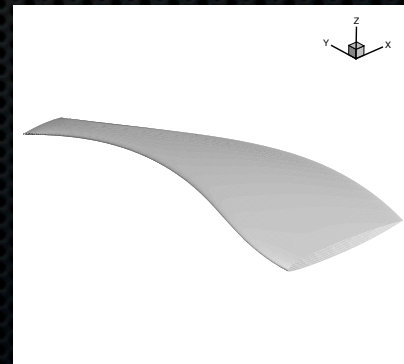
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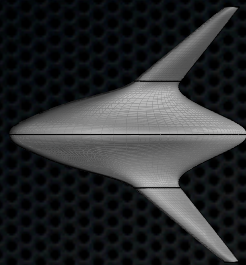
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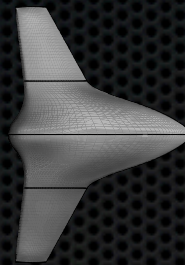
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# Multimodality

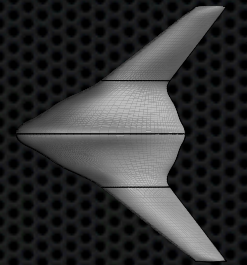
- BWB optimization: 8 local minima from 34 initial geometries using GB-MS



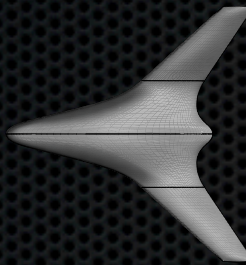
(a) Local Optimum 1



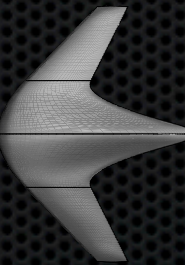
(b) Local Optimum 2



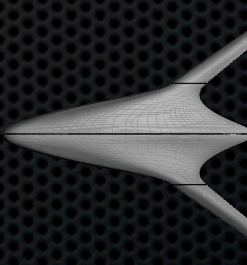
(c) Local Optimum 3



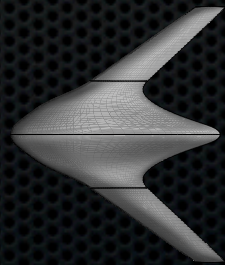
(d) Local Optimum 4



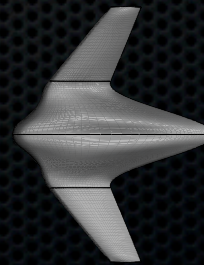
(e) Local Optimum 5



(f) Local Optimum 6



(g) Local Optimum 7



(h) Local Optimum 8

# Future Work

- improve speed and reliability of turbulent flow solver
- address issues in optimization based on turbulent flow
- address geometry, mesh, and optimization issues
- extend transition prediction to 3D
- incorporate into MDO framework